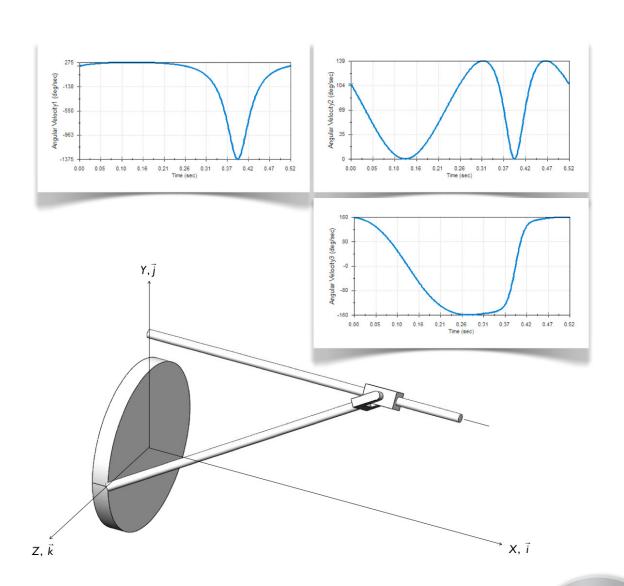
of the exercises in the book

Engineering Dynamics Labs

with SOLIDWORKS Motion 2015



Huei-Huang Lee



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Chapter I

Particle Kinematics

Rigid Body

In the real world, all solid bodies are more or less deformable. There are no such things as **rigid bodies**. However, if the deformation of a body is not our concern and if the deformation is negligible relative to the motion of the body, we can treat the body as a **rigid body**. In this book, we assume all bodies studied are **rigid bodies**. In rigid body dynamics, **springs** are the only elements that are deformable.

Particle

Similarly, in the real world, there are no such things as particles, which occupy zero volume in the space. However, when a body doesn't rotate (therefore no angular velocity, angular acceleration, angular kinetic energy, or angular momentum), we can treat the body as though its entire mass concentrates at its mass center and regard it as a **particle**.

Even when a body does rotate but its angular velocity remains constant, we still can treat the body as a particle, since its rotational quantities (angular velocity, angular acceleration, angular kinetic energy, or angular momentum) remain unchanged during the motion. For example, in the study of space mechanics, we often treat a planet as a particle, even though it does rotate. Keep in mind that a body is treated as a particle not because of its size, but because of its insignificance of rotation.

Chapters I-4 provide exercises on dynamic systems involving bodies that can be treated as particles.

Kinematics

What is kinematics? To answer this question, let's first explain how a dynamics problem is solved (either by computer or hand-calculation). Like any other engineering analysis, solving a dynamics problem involves two main steps: (a) write down a set of equations and (b) solve the equations.

For rigid body dynamics, these equations can be divided into two groups: (a) Equations based on **physical principles**. For each body, some equilibrium equations (e.g., Newton's 2nd Law) or conservation equations (e.g., principle of work and energy) can be written down. (b) Equations describing the **kinematics relations** among bodies. That is, the relations among motions of bodies. The motions of a particle can be fully described by its **position**, **velocity**, and **acceleration**.

Particle kinematics is the study of the relations among **positions**, **velocities**, and **accelerations** of particles involved in a dynamics system. Examples of kinematics problems are: (a) If a particle has an acceleration of $\vec{a}(t)$, what is its velocity $\vec{v}(t)$ and position $\vec{r}(t)$? (b) If particle A is moving with a constant acceleration of \vec{a}_A , what is the acceleration, velocity, and position of particle B at time t?

Chapter I provides exercises on particle kinematics.

Section I.I

Rectangular Components: Falling Ball



I.I-I Introduction

[1] Imagine that you throw a ball with an initial velocity [2-5]. The velocity and the position of the ball at time t = 1 sec can be calculated as follows.

In X-direction, the velocity component is constant,

$$v_x = v_0 \cos \theta = (5 \text{ m/s})(\cos 45^\circ) = 3.54 \text{ m/s}$$
 (1)

and the position is

$$X = (v_0 \cos \theta)t = (5 \text{ m/s})(\cos 45^\circ)(1 \text{ s}) = 3.54 \text{ m}$$
 (2)

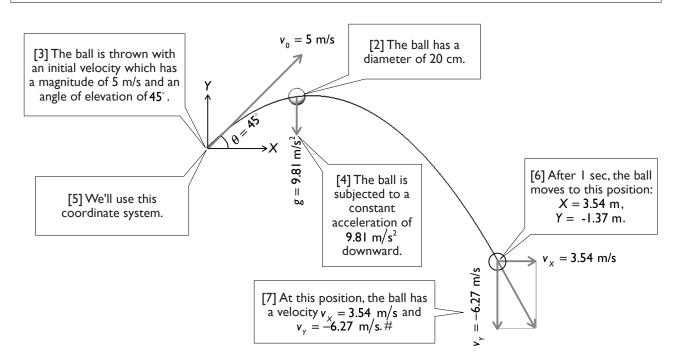
In Y-direction, the velocity component is

$$v_y = v_0 \sin \theta - gt = (5 \text{ m/s})(\sin 45^\circ) - (9.81 \text{ m/s}^2)(1 \text{ s}) = -6.27 \text{ m/s}$$
 (3)

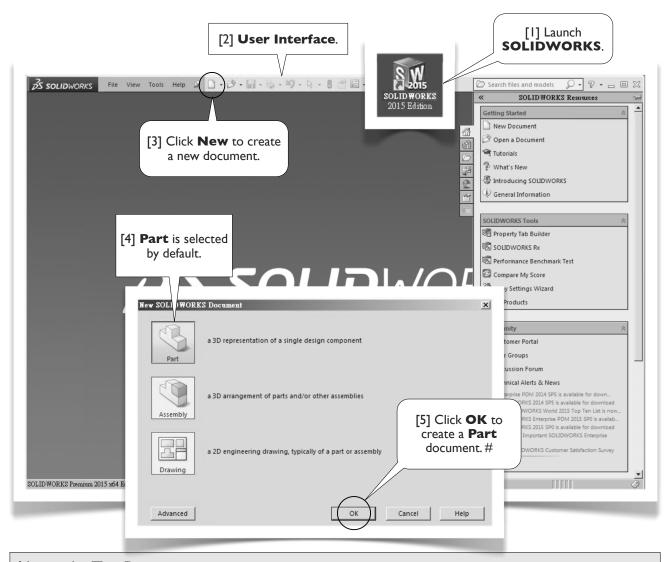
and the position is

$$Y = (v_0 \sin \theta)t - \frac{1}{2}gt^2 = (5 \text{ m/s})(\sin 45^\circ)(1 \text{ s}) - \frac{1}{2}(9.81 \text{ m/s}^2)(1 \text{ s})^2 = -1.37 \text{ m}$$
 (4)

These values are shown in [6, 7]. In this section, we'll perform a simulation for this scenario and validate the simulation results with the values in Eqs. (1-4).



1.1-2 Launch **SOLIDWORKS** and Create a New Part



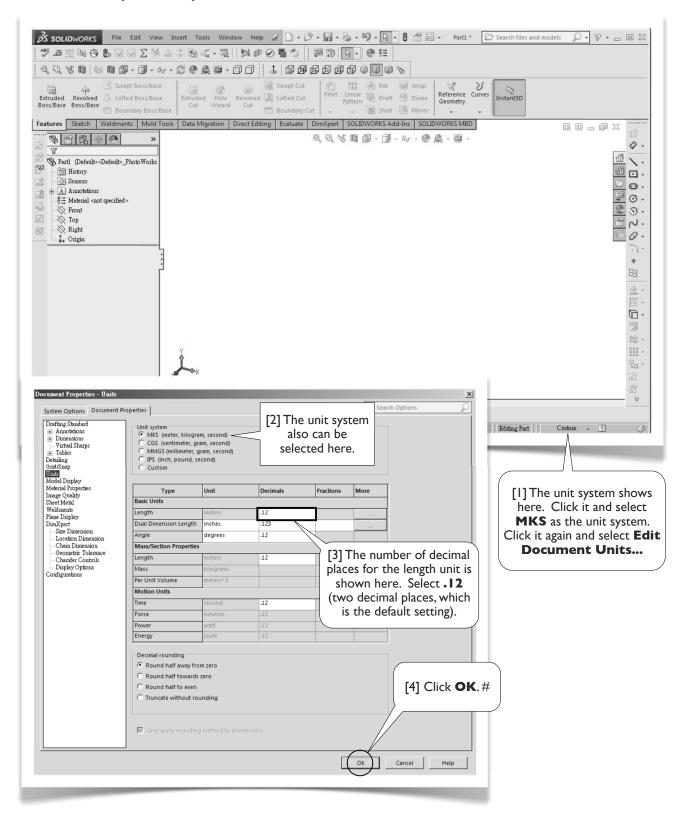
About the TextBoxes

- I. Within each subsection (e.g., I.I-2), textboxes are ordered with numbers, each of which is enclosed by a pair of square brackets (e.g., [1]). When you read the contents of a subsection, please follow the order of the textboxes.
- 2. The textbox numbers are also used as reference numbers. Inside a subsection, we simply refer to a textbox by its number (e.g., [1]). From other subsections, we refer to a textbox by its subsection identifier and the textbox number (e.g., 1.1-2[1]).
- 3. A textbox is either round-cornered (e.g., [1, 3, 5]) or sharp-cornered (e.g., [2, 4]). A round-cornered textbox indicates that **mouse or keyboard actions** are needed in that step. A sharp-cornered textbox is used for commentary only; i.e., mouse or keyboard actions are not needed in that step.
- 4. A symbol # is used to indicate the last textbox of a subsection [5], so that you don't leave out any textboxes.

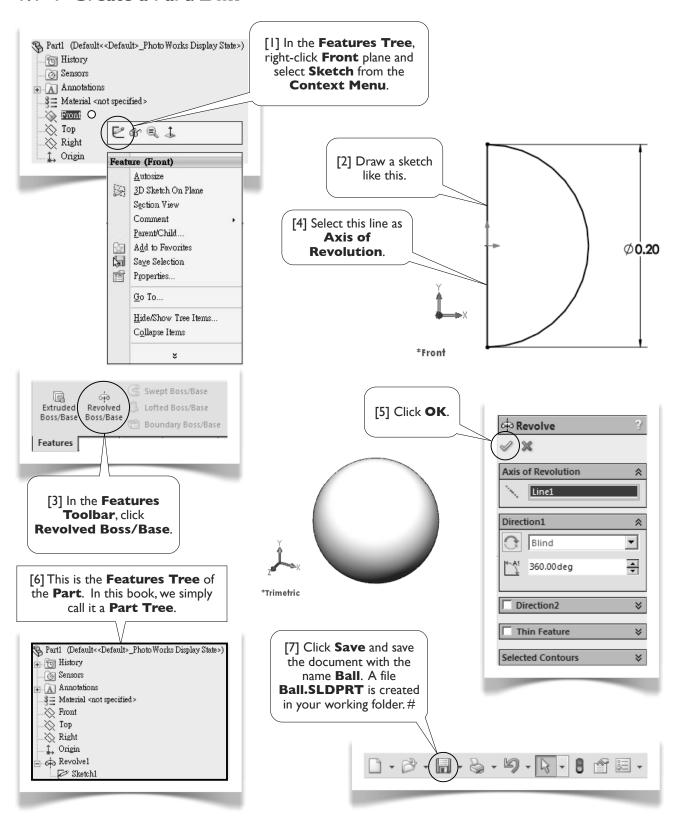
SOLIDWORKS Terms

In this book, terms used in the **SOLIDWORKS** are boldfaced (e.g., **Part** in [4, 5]) to facilitate the readability.

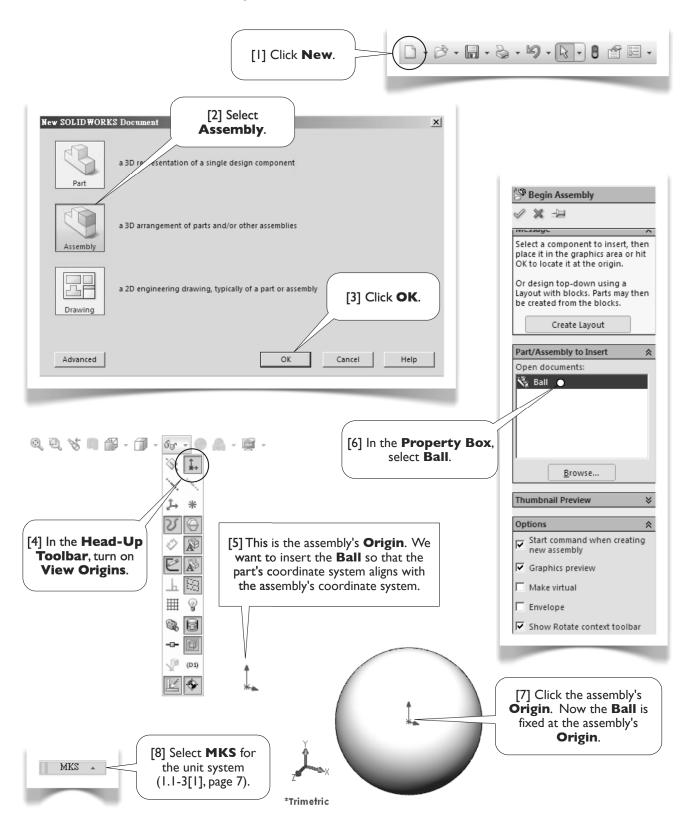
I.I-3 Set Up Unit System

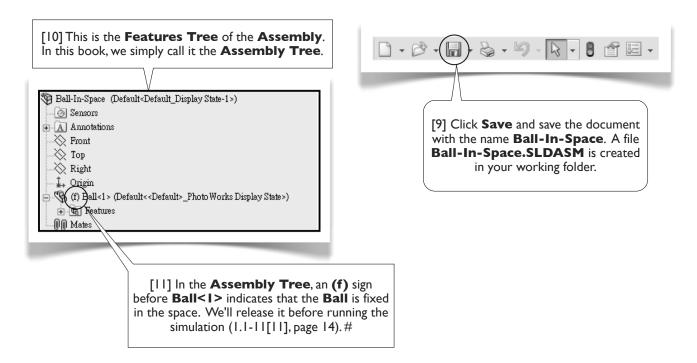


1.1-4 Create a Part: Ball

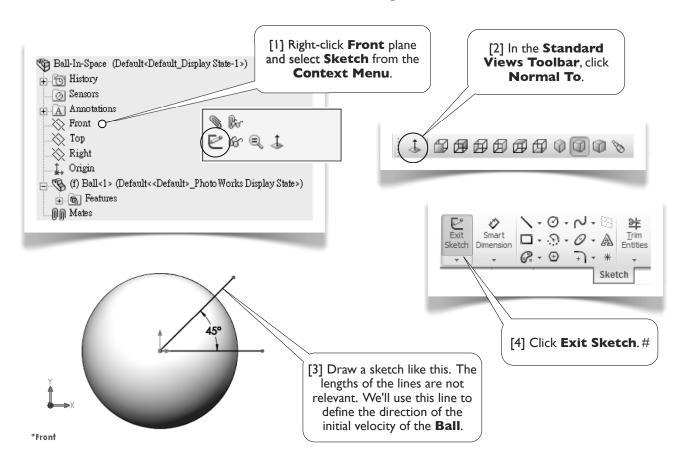


1.1-5 Create an Assembly: Ball-In-Space

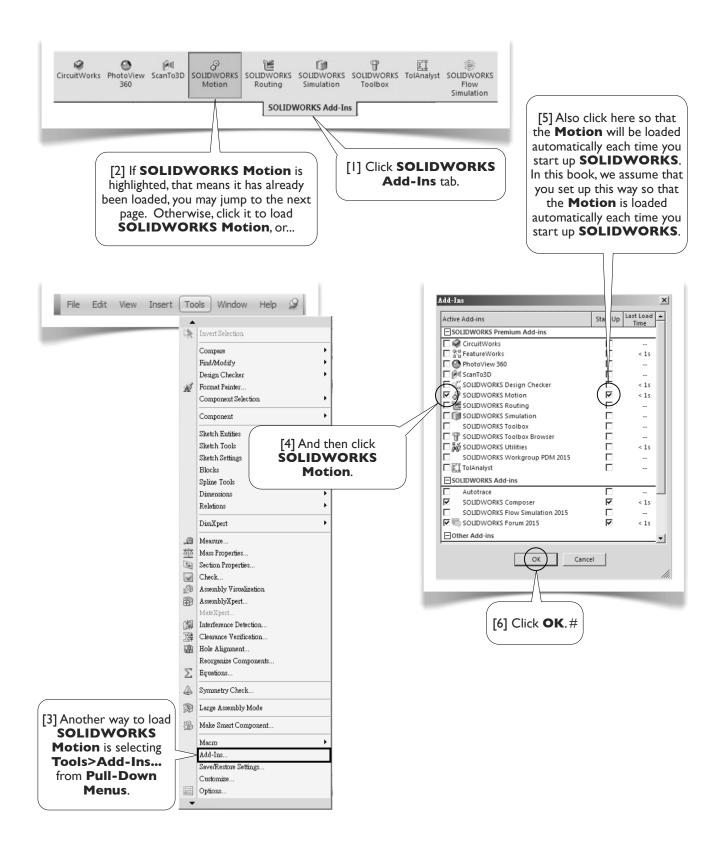




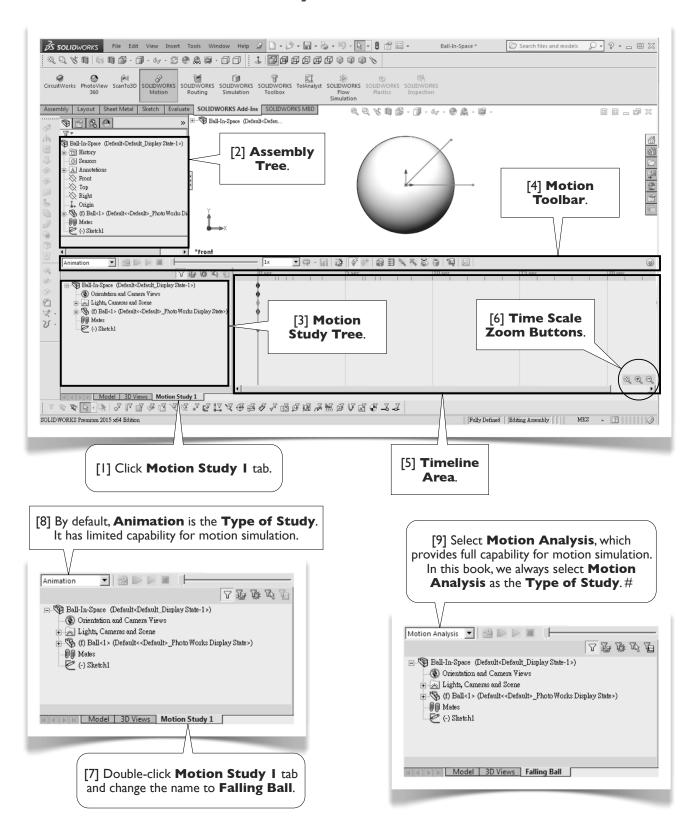
1.1-6 Create a **Sketch** in the **Assembly**

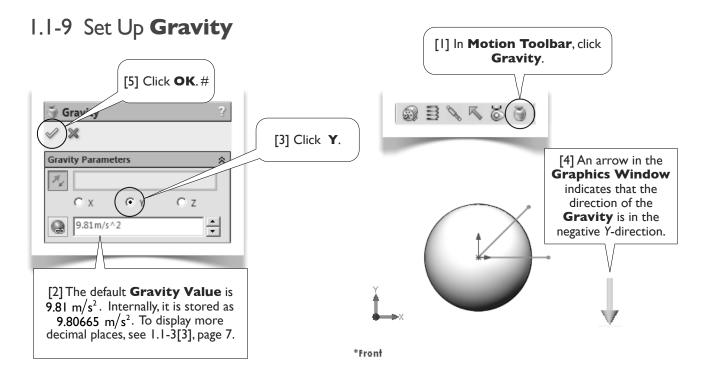


1.1-7 Load SOLIDWORKS Motion

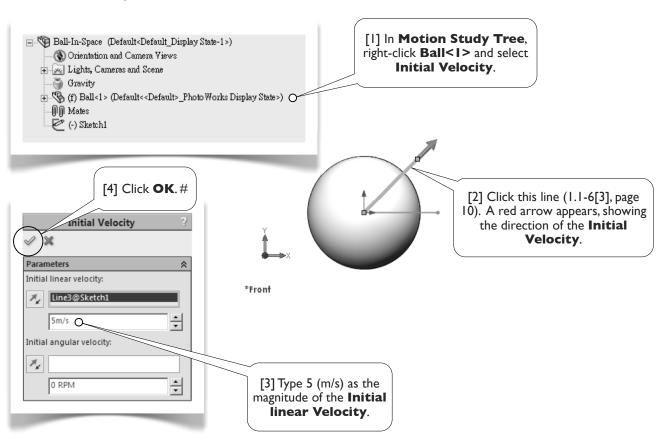


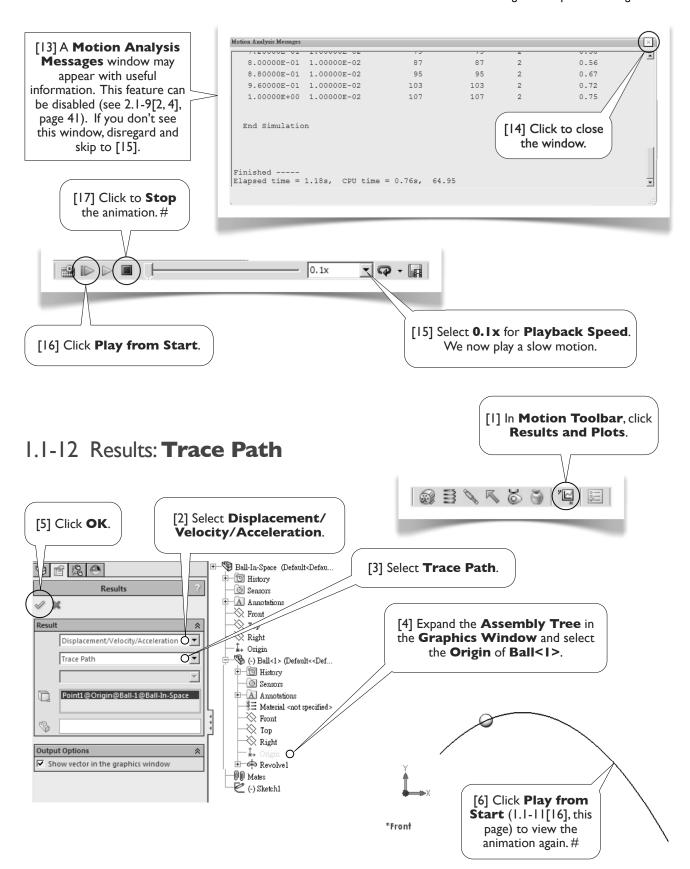
1.1-8 Create a **Motion Study**



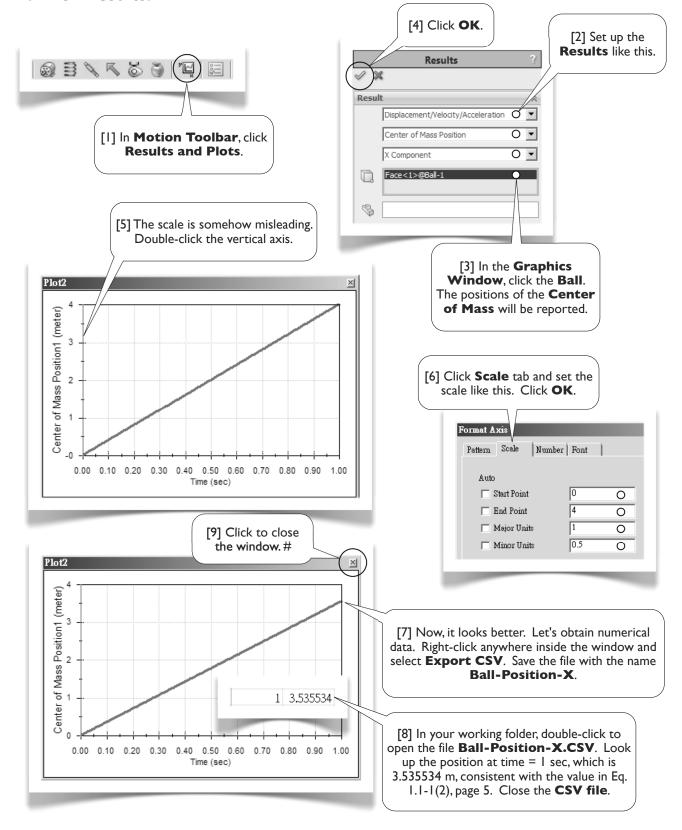


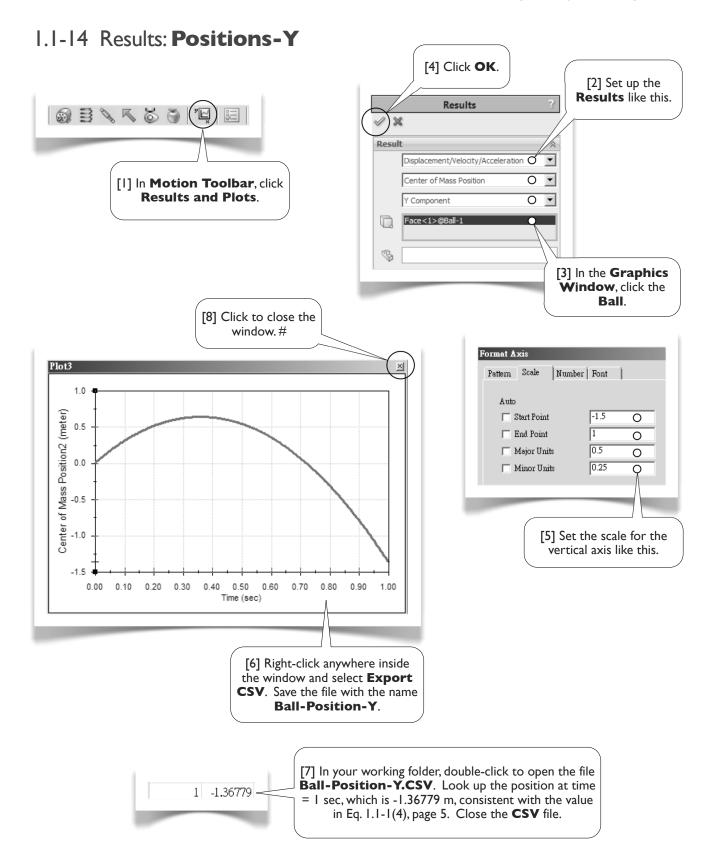
I.I-I0 Set Up Initial Velocity for the Ball



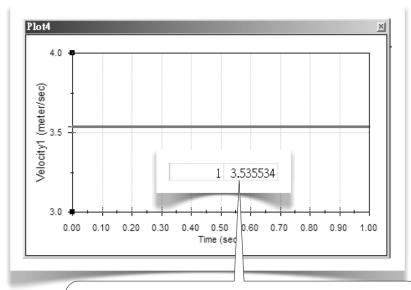


1.1-13 Results: Positions-X

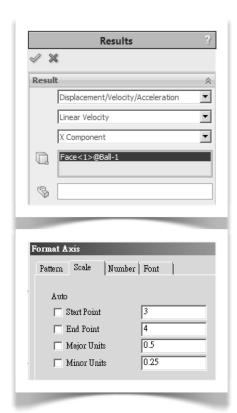




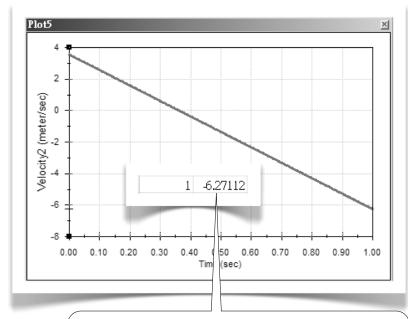
I.I-I5 Results: **Velocity-X**



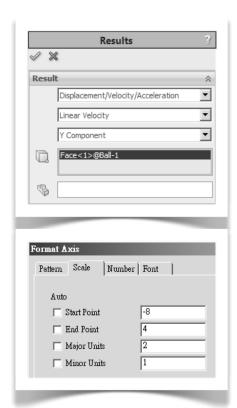
[1] Follow a similar procedure in 1.1-14 to obtain the **Ball's** velocity in X-direction, which is a constant (3.535534 m/s) over the time, consistent with the value in Eq. 1.1-1(1), page 5.#

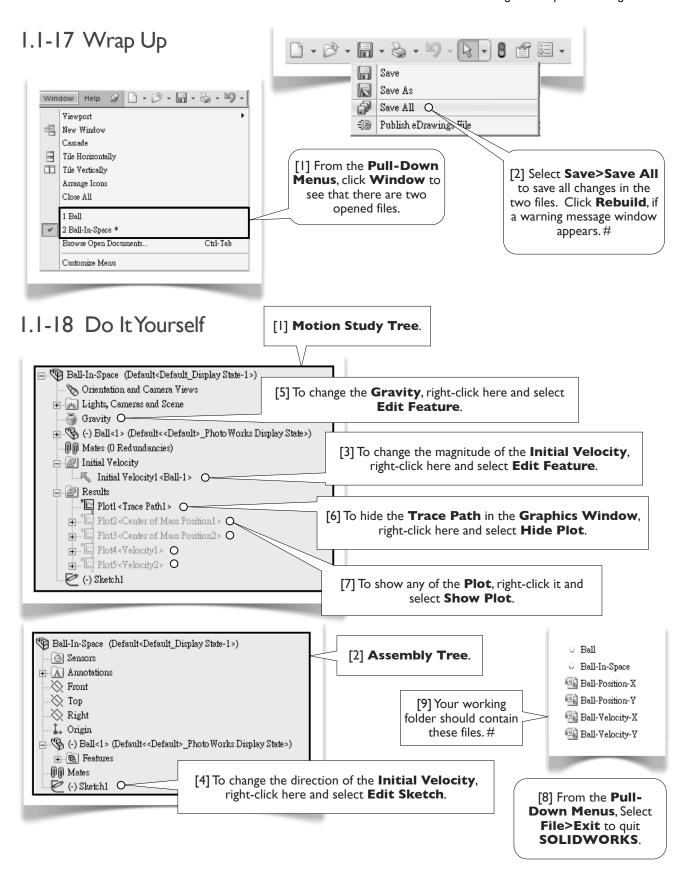


1.1-16 Results: **Velocity-Y**



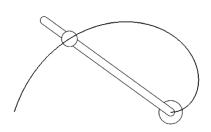
[1] Follow a similar procedure in 1.1-14 to obtain the **Ball's** velocity in Y-direction, which is -6.27112 m/s at time = 1 sec, consistent with the value in Eq. 1.1-1(3), page 5.#





Section 1.2

Radial and Transverse Components: Sliding Collar on Rotating Arm



1.2-1 Introduction

[1] Consider an **Arm** rotating about a **Pivot** with an angular speed $\dot{\theta} = \pi$ rad/s [2-4]. A **Collar** initially aligned with the **Pivot** slides along the **Arm** with a constant speed $\dot{r} = 1.0$ m/s [5-6].

Let's use a polar coordinate system centered at the **Pivot** and let (r, θ) be the position of the **Collar's** center. Denote \vec{e}_r the unit vector in radial direction and \vec{e}_θ the unit vector in transversal direction [7, 8]. Then the position, velocity, and acceleration of the **Collar's** center are respectively

$$\vec{r} = r\vec{e}_{r}$$

$$\vec{v} = \dot{r}\vec{e}_{r} + r\dot{\theta}\vec{e}_{\theta}$$

$$\vec{a} = (\ddot{r} - r\dot{\theta}^{2})\vec{e}_{r} + (r\ddot{\theta} + 2\dot{r}\dot{\theta})\vec{e}_{\theta}$$
(1)

Let's calculate these values at an arbitrary time, say t = 0.8 s. At that time [9, 10],

$$r=0.8 \text{ m}$$
 $\theta=0.8\pi$
 $\dot{r}=1.0 \text{ m/s}$ $\dot{\theta}=\pi \text{ rad/s}$
 $\ddot{r}=0 \text{ m/s}^2$ $\ddot{\theta}=0 \text{ rad/s}^2$

Then, the position is

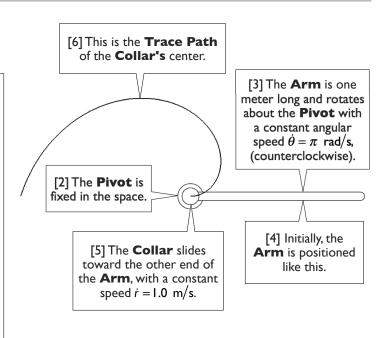
$$\vec{r} = r\vec{e}_{r}$$

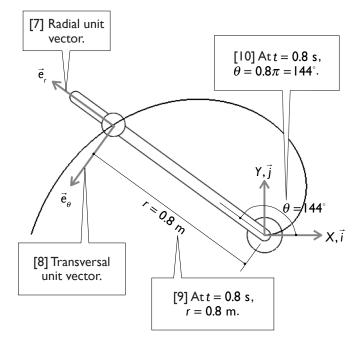
$$= 0.8\vec{e}_{r}$$

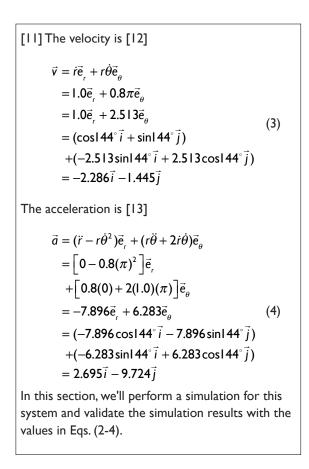
$$= 0.8(\cos 44^{\circ})\vec{i} + 0.8(\sin 44^{\circ})\vec{j}$$

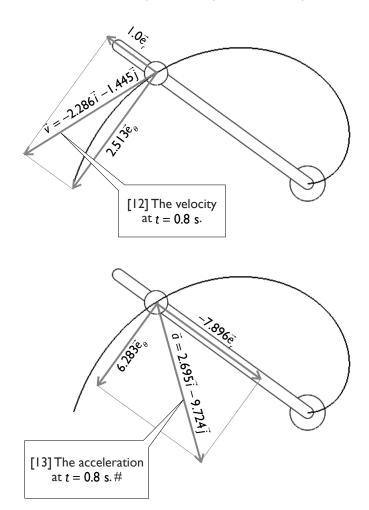
$$= -0.647\vec{i} + 0.470\vec{j}$$
(2)

where \vec{i} is the unit vector in X-direction and \vec{j} is the unit vector in Y-direction. The origin of the XY-coordinate system is the same as that of the polar coordinate system.

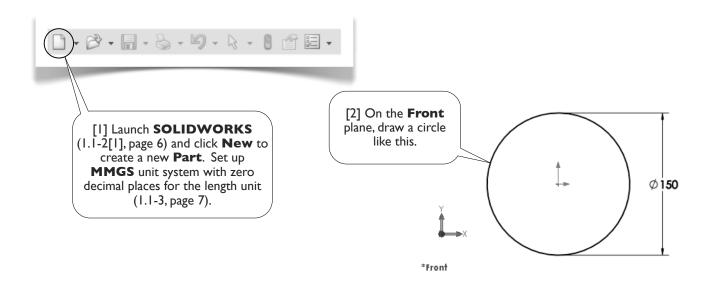


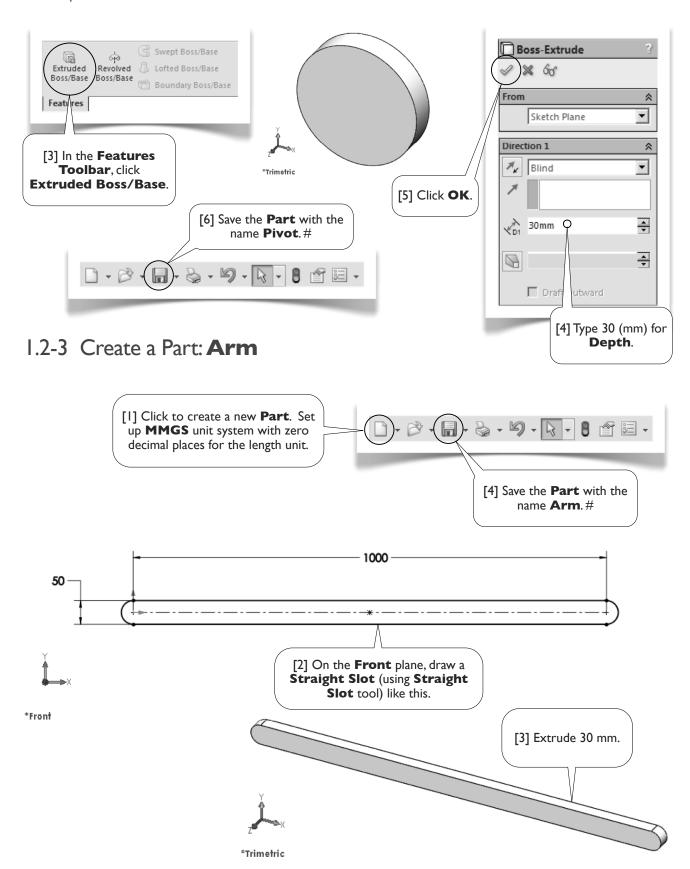


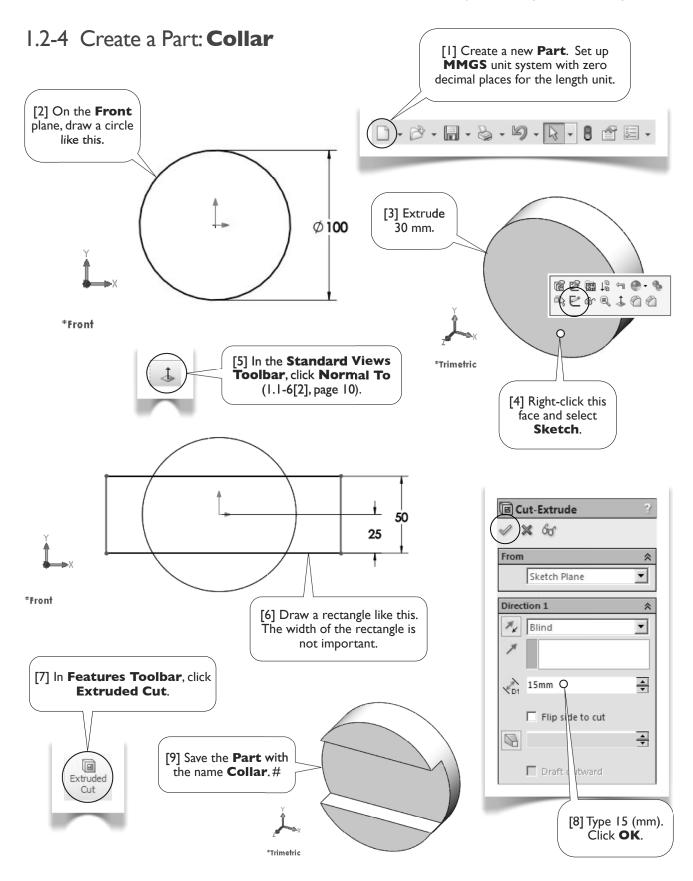




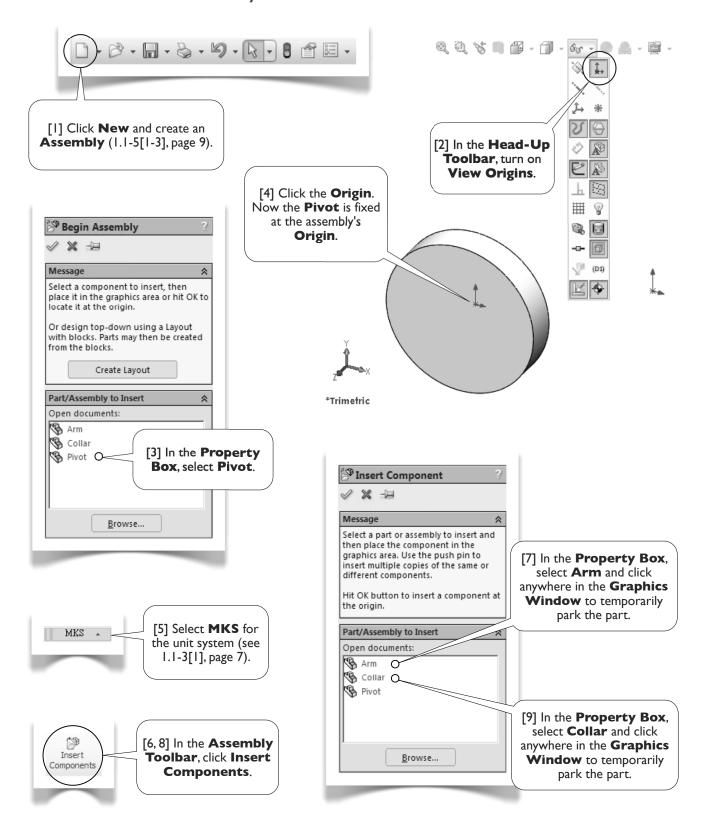
1.2-2 Start Up and Create a Part: Pivot

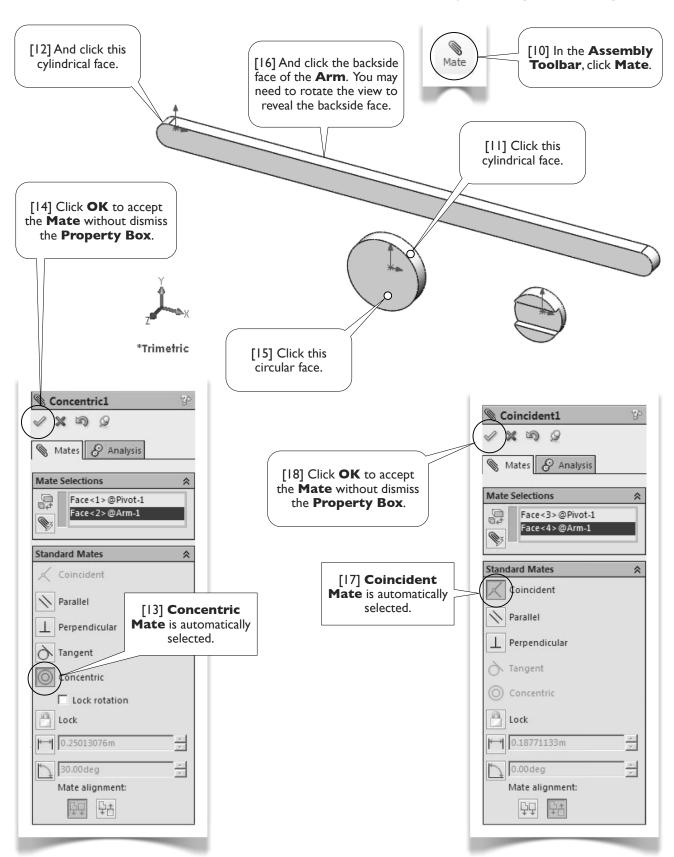




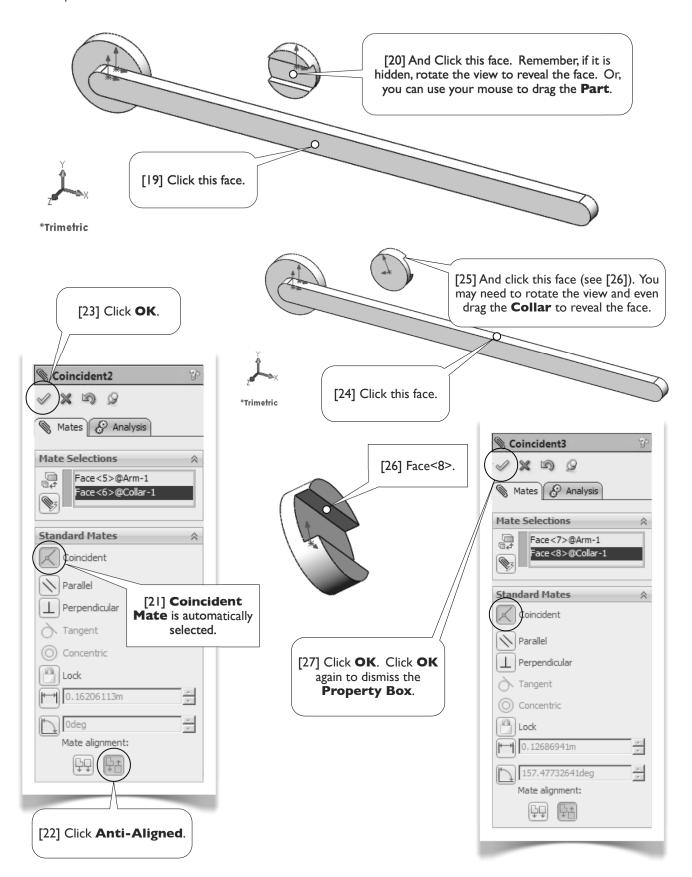


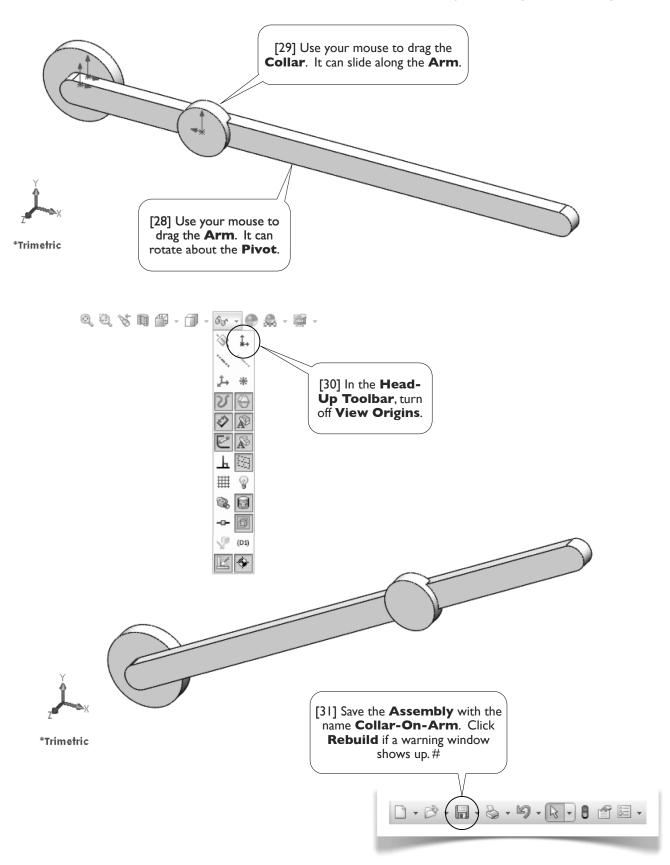
1.2-5 Create an Assembly: Collar-On-Arm

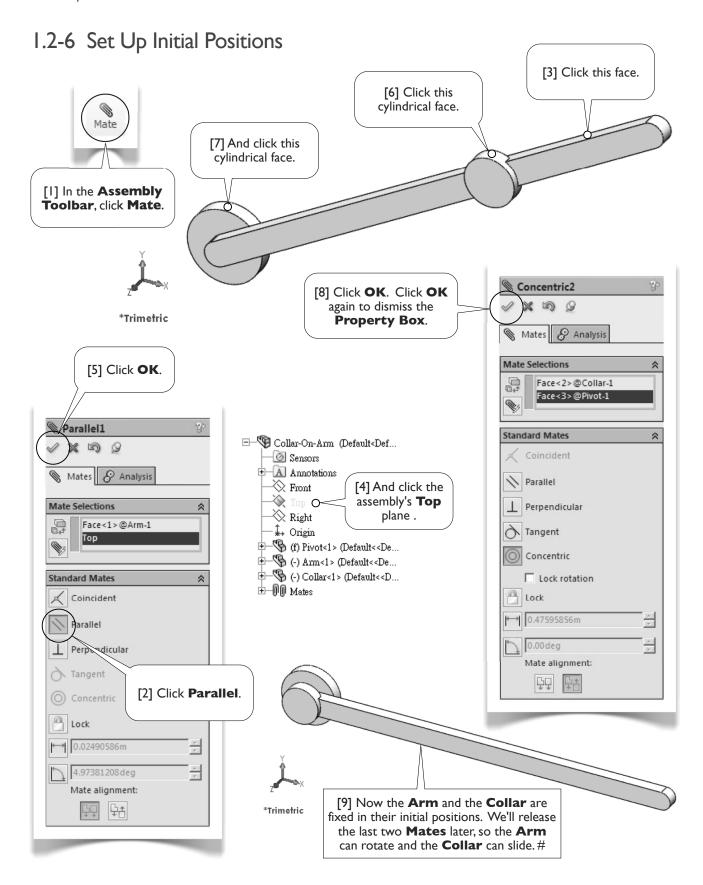




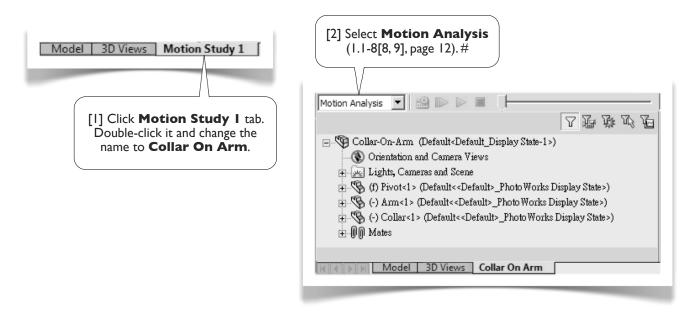




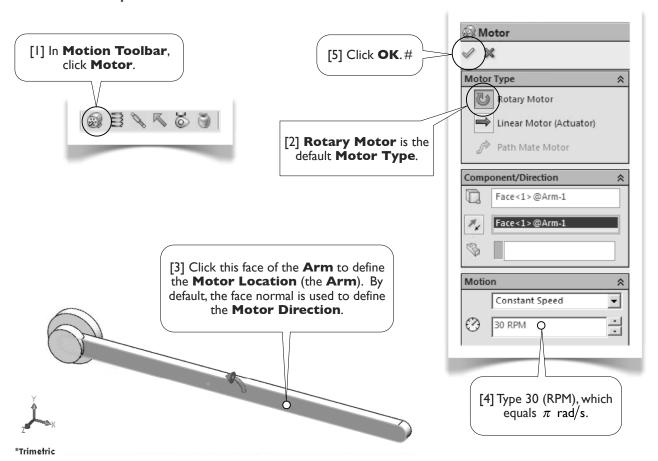




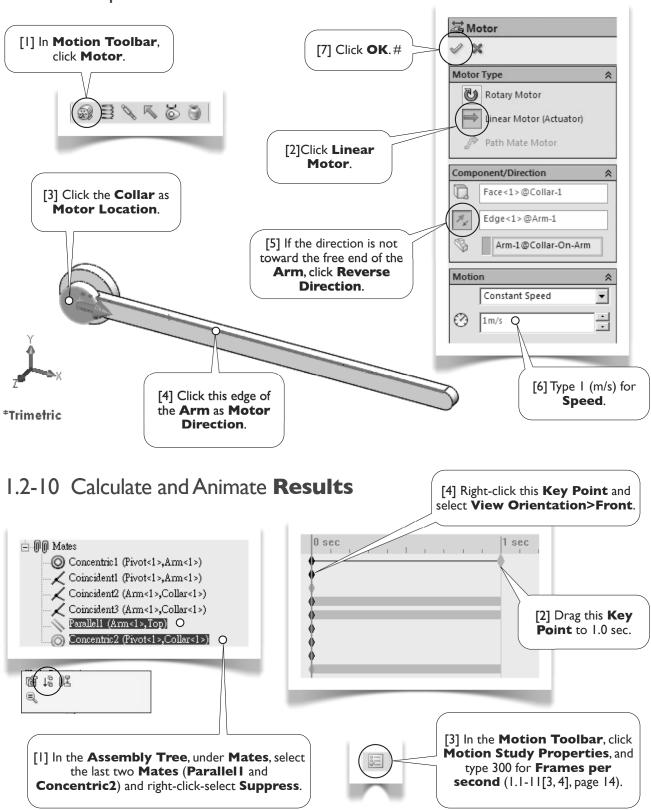
1.2-7 Create a Motion Study

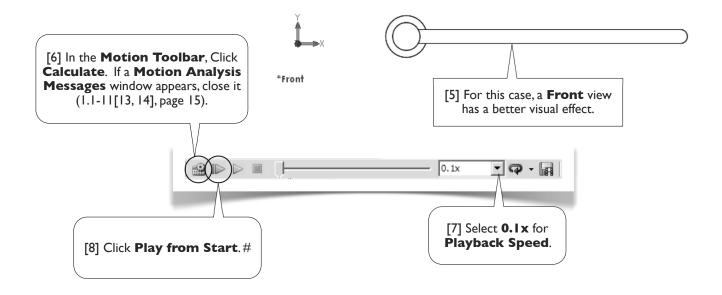


1.2-8 Set Up Motor at the Arm

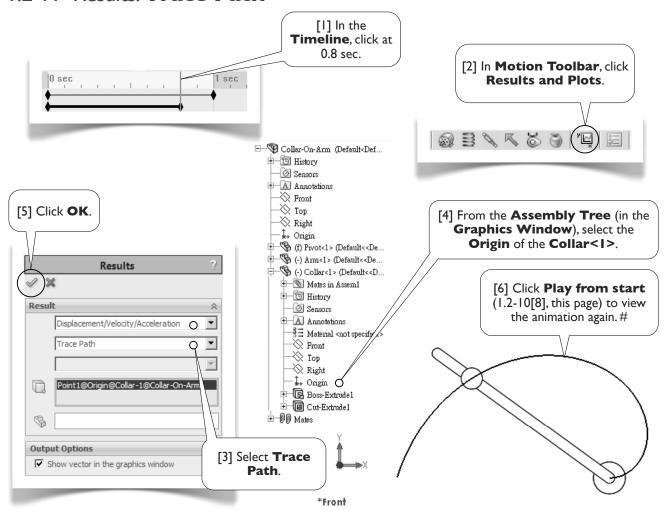


1.2-9 Set Up Motor at the Collar

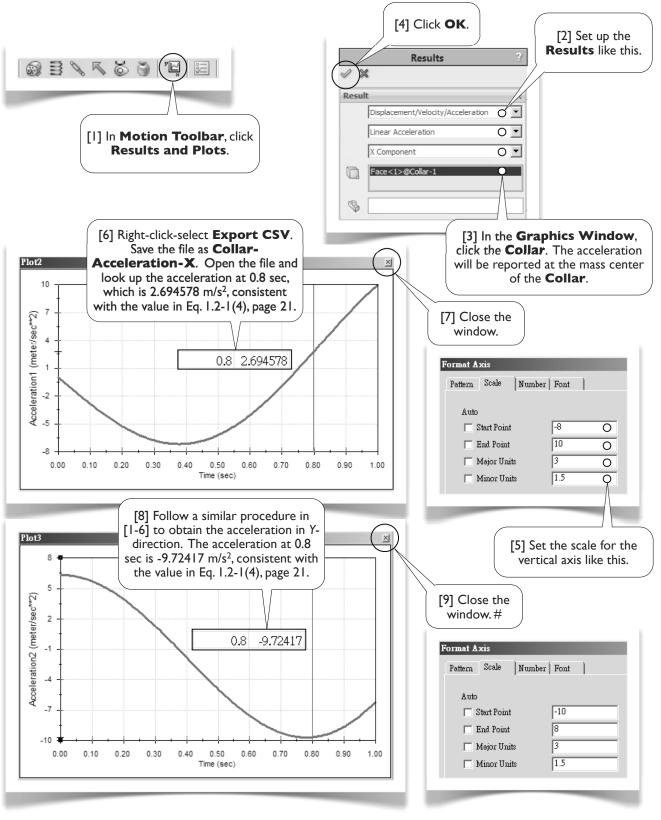




1.2-11 Results: Trace Path

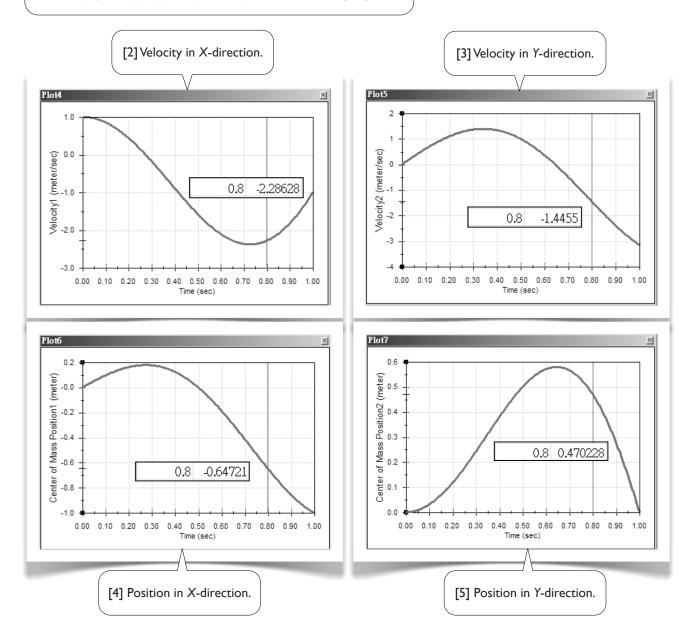


1.2-12 Results: Acceleration



1.2-13 Do It Yourself

[1] We leave you to obtain the velocities (Eq. 1.2-1(3), page 21) and the positions (Eq. 1.2-1(2), page 20). These plots are shown in [2-5].



Wrap Up

[6] Save all files and exit **SOLIDWORKS** (1.1-18[1-3], page 19).#