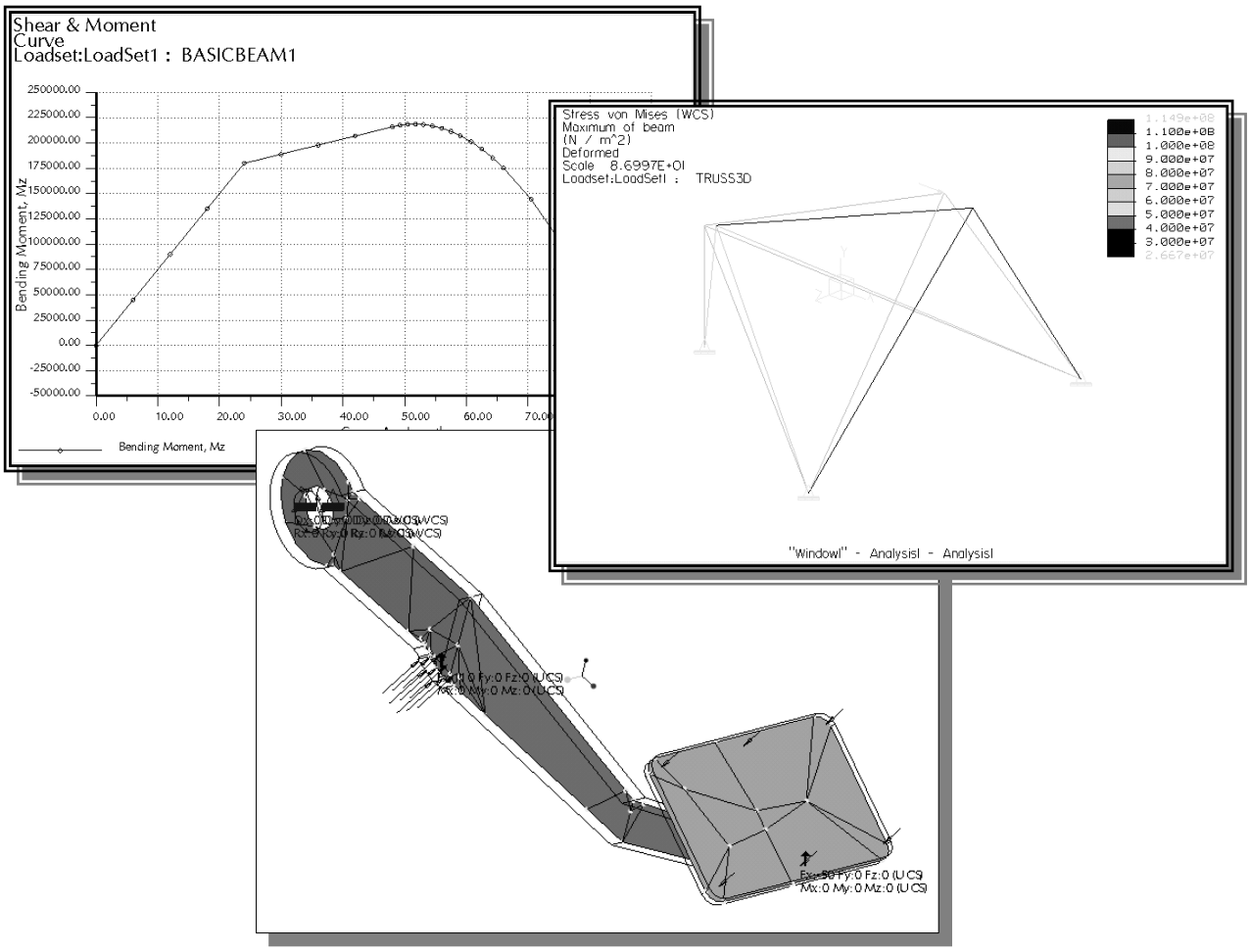
# Introduction to Finite Element Analysis

## Using Pro/MECHANICA Wildfire 4.0®

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