

An Introduction to Numerical Methods Using MATLAB®

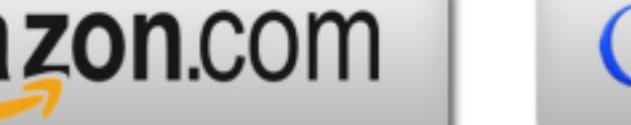


Khyruddin Akbar Ansari, Ph.D., P.E.
Bonni Dichone, Ph.D.



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